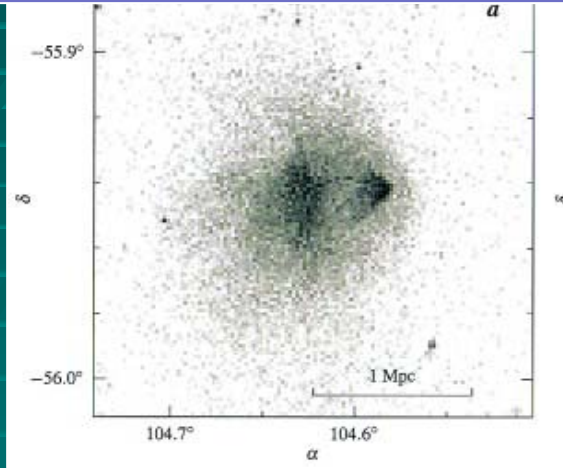


**N-body + Hydrodynamical
Simulations of Merging
Clusters of Galaxies:
Comparison with 1E0657-56**

Motokazu Takizawa
(Yamagata University, Japan)

1E 0657-56 Cluster

X-ray image
(Markevitch et al. 2002)

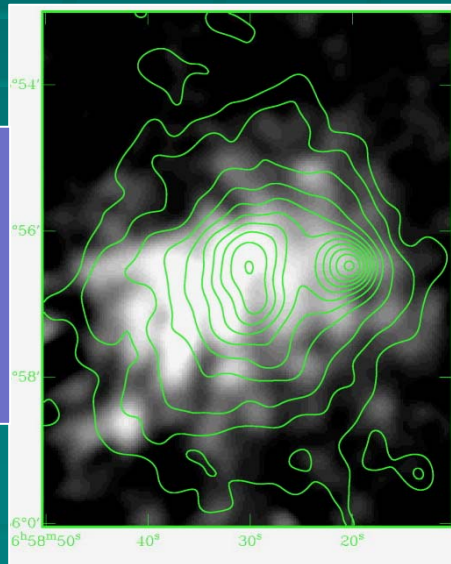


- $z=0.296$
- The hottest known cluster ($\sim 17\text{keV}$)
- A very powerful radio halo
- First observational example of shocks in ICM
- Mass map through weak gravitational lensing

Liang et al. (2000)

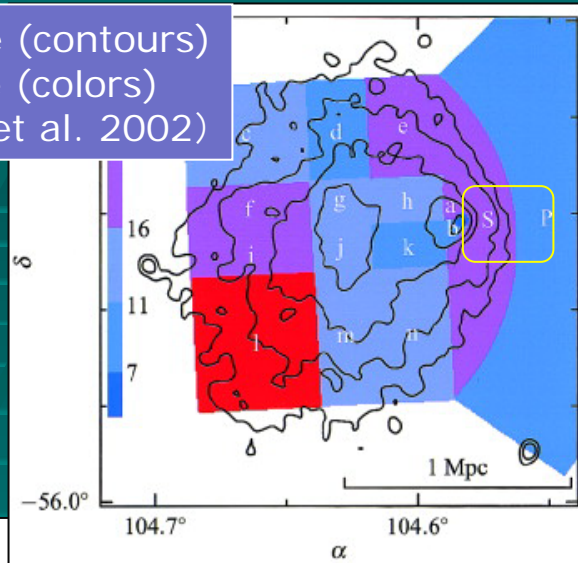
Contour: X-ray
(ROSAT HRI)

Gray scale: radio

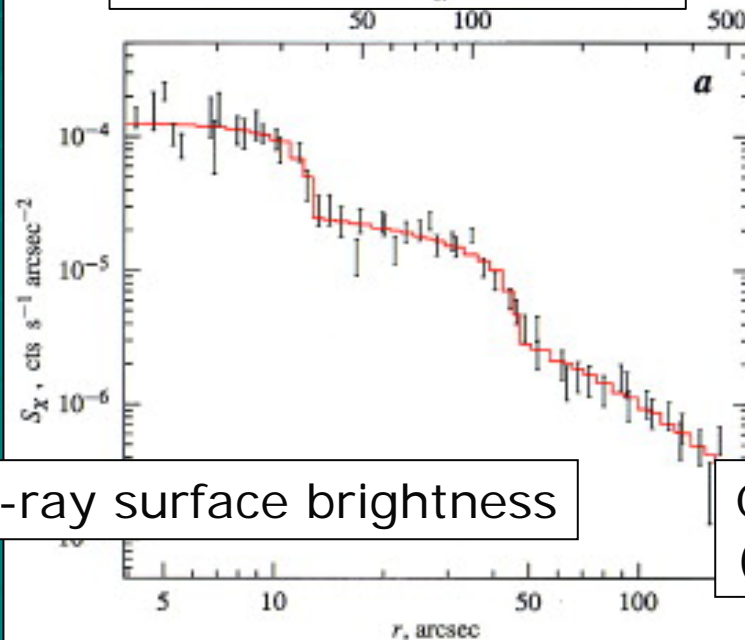


1E 0657-56: cold front & bow shock

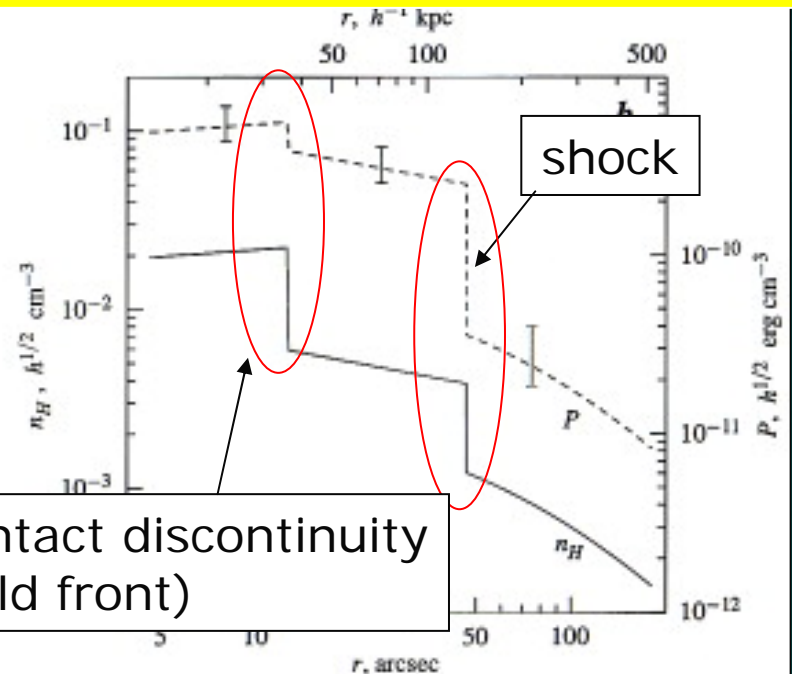
X-ray image (contours)
Temperature (colors)
Markevitch et al. 2002



Density and pressure profiles in front of the substructure

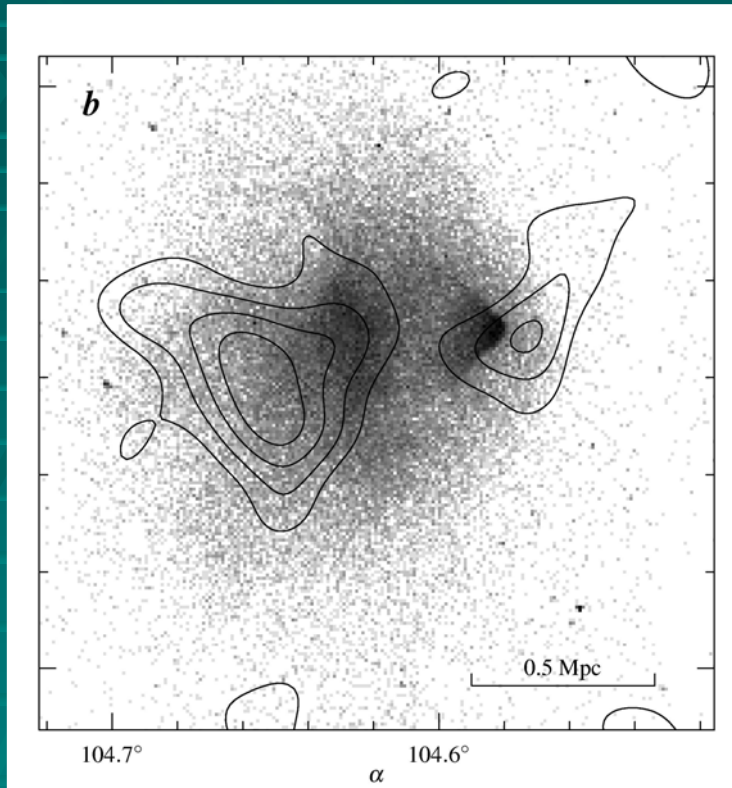


X-ray surface brightness



Contact discontinuity
(cold front)

1E 0657-56: mass distribution



X-ray image(gray scale)
Surface mass density(contours)
Clowe et al.(2004)

- Mass distribution is investigated through weak lensing.
- Clear offsets of the mass density peaks from the X-ray peaks are found.
- Distribution of the member galaxies is quite similar to that of mass.

Does this structure occur because the ICM experiences ram pressure but the dark matter and galaxies do not ?

Numerical Method (N-body+Hydro)

- N-body: Particle Mesh(PM) method
- Self-gravity: FFT with isolated boundary conditions
- Hydrodynamics: Roe TVD method
 - zero gradient boundary conditions (but, only outflow is permitted)
- Number of the grid points $256 \times 128 \times 128$
- Number of the N-body particles $256 \times 128 \times 128 (\doteq 4.2 \times 10^6)$
- VPP5000@NAOJ

Virialized Cluster Model

- DM: NFW model, ICM: β model ($r_c=r_s/2$)

DM density profile

$$\rho_{\text{DM}}(r) = \frac{\delta_c \rho_{c0}}{(r/r_s)(1+r/r_s)^2}$$

ICM density profile

$$\rho_g(r) = \rho_{g,0} \left\{ 1 + \left(\frac{r}{r_c} \right)^2 \right\}^{-\frac{3}{2}\beta}$$

- $r \geq r_{\text{vir}}$ $\rho_{\text{DM}} = 0$ and $\rho_{\text{gas}} = \text{constant}$
- DM velocity distribution is an isotropic Maxwellian. Radial profile of DM velocity dispersion is determined from the Jeans equation.

$$\frac{d}{dr} (\rho_{\text{DM}} \sigma^2) = -\frac{GM_r}{r^2} \rho_{\text{DM}}$$

with

$$\sigma^2(r_{\text{out}}) = \frac{GM_r}{3r} \Big|_{r=r_{\text{out}}}$$

- Radial profile of ICM pressure is determined from the hydrostatic equation.

$$\frac{dP}{dr} = -\frac{GM_r}{r^2} \rho_g$$

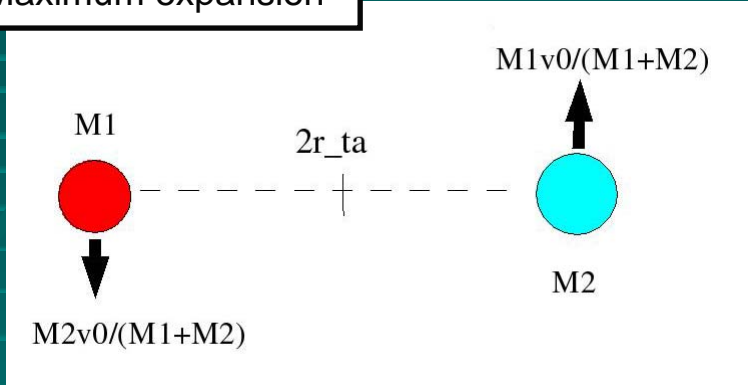
with

$$P(r_{\text{out}}) = \frac{1}{\beta} \frac{GM_r \rho_g}{3r} \Big|_{r=r_{\text{out}}}$$

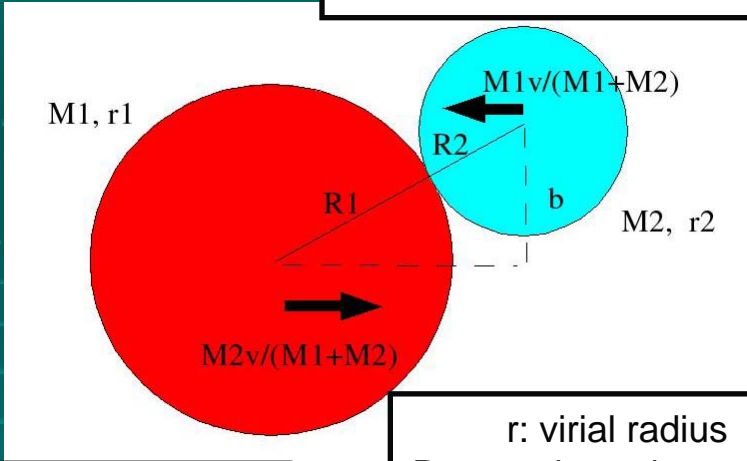
- $r \leq r_{\text{out}}$ $M_{\text{gas}} / (M_{\text{gas}} + M_{\text{DM}}) = 0.1$

How to make initial conditions for mergers

Maximum expansion



Initial state for simulations



r: virial radius
R: outer boundary radius

energy conservation
Angular momentum conservations

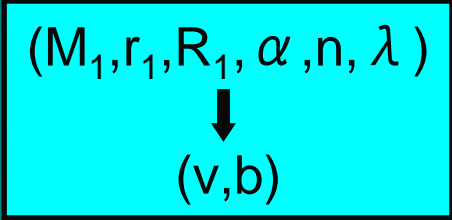
$$-\frac{GM_1M_2}{2r_{ta}} + \frac{1}{2}Mv_0^2 = -\frac{GM_1M_2}{R_1 + R_2} + \frac{1}{2}Mv^2$$

$$2Mv_0r_{ta} = Mvb$$

Using scaling relation $R \propto M^{(5+n)/6}$ and $r_{ta} = 2 r_{vir}$ (Spherical collapse model), we obtain the following equations

$$v^2 = \frac{2GM_1}{R_1} (1 + \alpha) \left\{ \frac{1}{1 + \alpha^{(5+n)/6}} - \frac{1}{4(1 + \alpha)^{(5+n)/6}} \frac{R_1}{r_1} \right\} \left\{ 1 - \frac{1}{16(1 + \alpha)^{(5+n)/3}} \left(\frac{b}{r_1} \right)^2 \right\}^{-1}$$

$$\alpha = \frac{M_2}{M_1}$$



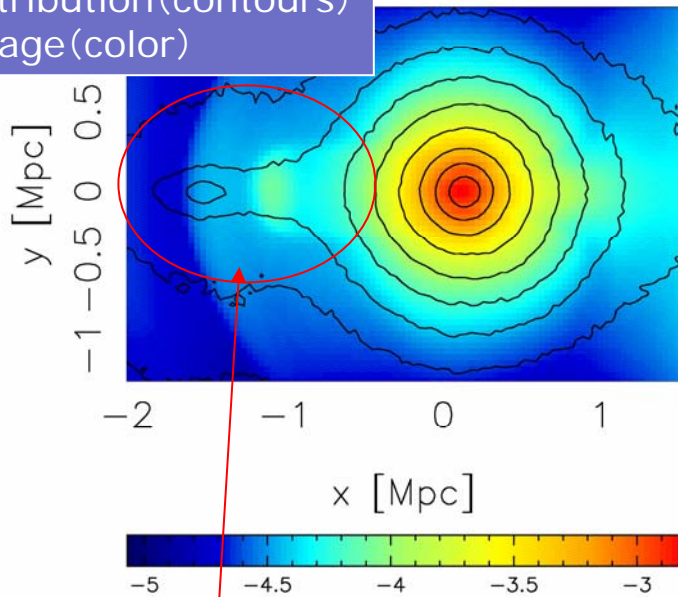
$$\lambda \equiv \frac{J|E|^{1/2}}{G(M_1 + M_2)^{5/2}} = \frac{vb}{(GM_1R_1)^{1/2}} \frac{\alpha^{3/2}}{(1 + \alpha)^{7/2}} \left\{ \frac{1}{1 + \alpha^{(5+n)/6}} - \frac{R_1v^2}{2GM_1} \frac{1}{1 + \alpha} \right\}^{1/2}$$

Comparison with 1E0657-56

Head on merger with mass ratio=16:1,
1Gyr after the core passage

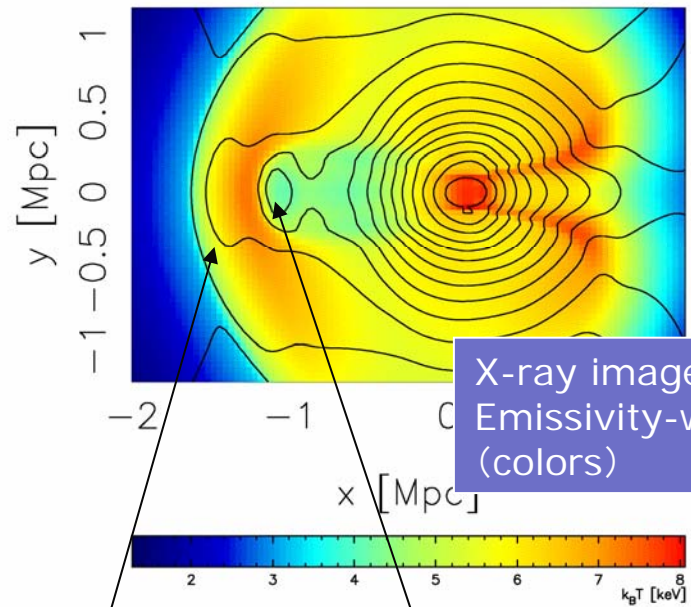
(a) mass vs X-ray

Mass distribution (contours)
X-ray image (color)



X-ray peak lagged behind mass peak

(b) X-ray vs kT_{ew}



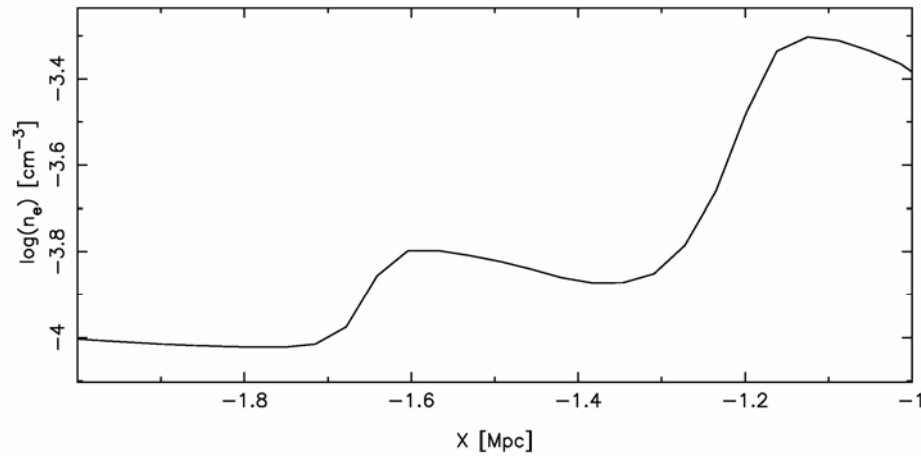
X-ray image (contours)
Emissivity-weighted kT_{ew}
(colors)

Bow shock

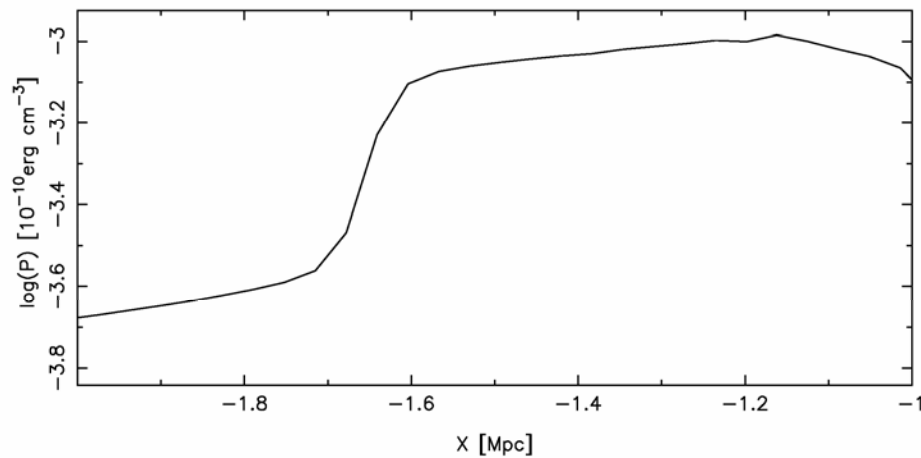
Cold front
(contact discontinuity)

Bow shock and Cold Front

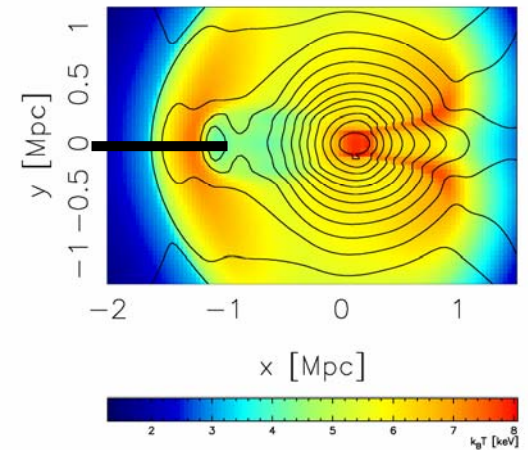
(a) Density



(b) Pressure



(b) X-ray vs kT_{ew}



Discussion on the Rum Pressure Stripping Conditions (1)

Consider the head-on merger of two NFW clusters with masses M_1 and M_2 ($M_1 > M_2$). If the gravity on the subcluster's ICM is weaker than the rum pressure force, the ICM will be stripped from the subcluster's potential.

$$\frac{Gm_2\rho_2}{r_2^2} < A(\pi r_2^2 \rho_1 v^2) \left(\frac{4}{3}\pi r_2^3\right)^{-1},$$

$r_{1,2}$: virial radius $\rho_{1,2}$: central gas density r_2 : scale radius m_2 : mass inside r_2
 A: fudge factor of an order of unity, likely $A < 1$

Collision velocity v

$$v^2 \simeq \frac{2G(M_1 + M_2)}{R_1 + R_2},$$

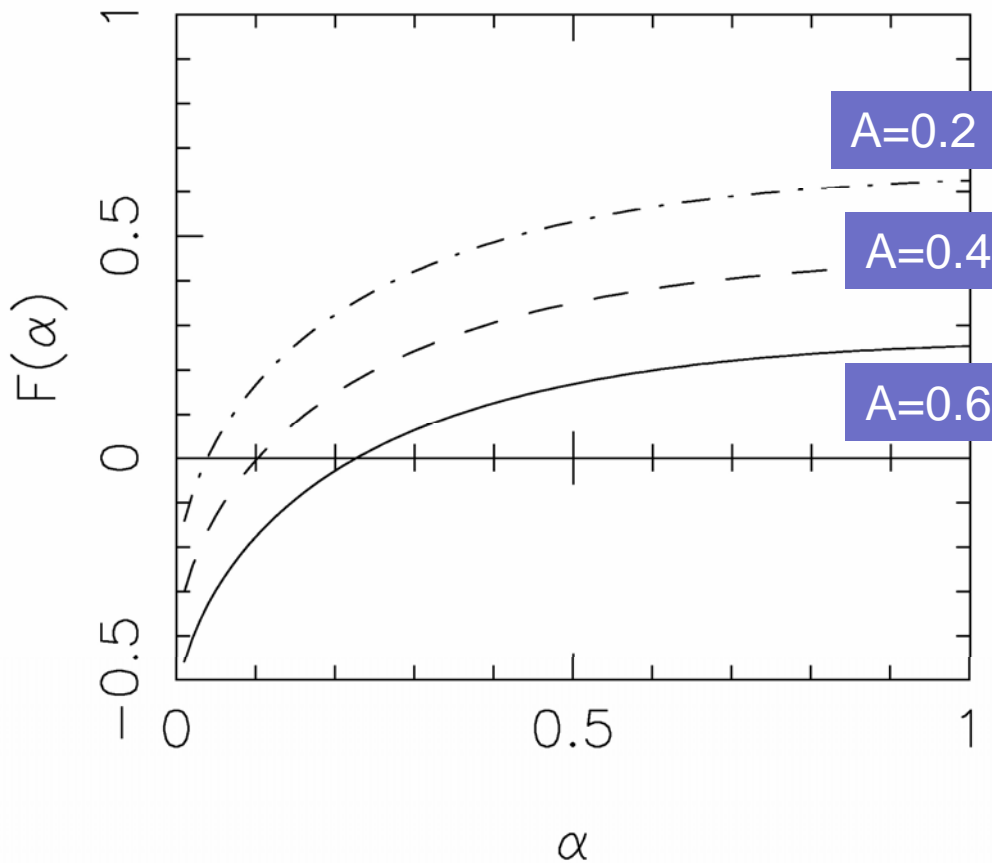
Introduce a new parameter $\alpha \equiv M_2/M_1$. Then, $R_2/R_1 = \alpha^{1/3}$, $\rho_1/\rho_2 = \alpha^{-x}$ (in the Λ CDM, $x \sim 0.25$). The above-mentioned condition becomes

$$F(\alpha : M_1) \equiv \alpha^{2/3-x} \frac{1 + \alpha^{1/3}}{1 + \alpha} - \frac{3A}{2g(\alpha M_1)c(\alpha M_1)} < 0.$$

$c = r_2/R_2$: concentration parameter

$$g(M_2) \equiv \frac{m_2}{M_2} = \frac{\ln 2 - 1/2}{\ln(1+c) - c/(1+c)},$$

Discussion on the Ram Pressure Stripping Conditions (2)



$F(\alpha) < 0$: ram pressure dominant

$$\alpha = M_2/M_1$$

When α is less than ~ 0.1 , ram pressure dominates the gravity.

ICM is more easily stripped from the less massive subcluster.

Discussion on the Ram Pressure Stripping Conditions (3)

- Ram pressure \ll gravity
 - Gas behaves like DM.
 - DM peaks will correspond with X-ray peaks.
- Ram pressure \gg gravity
 - ICM in the substructure cannot penetrate the larger cluster's center.
 - The larger cluster's ICM is so hot that it cannot be bound by the substructure's potential.
 - Mass peaks are associated with no X-ray peaks.
- Ram pressure \doteq gravity
 - Clear off-set of the mass peak from the X-ray peak

Summary

- We study dynamical evolution of merging clusters of galaxies using N-body + hydrodynamical simulations.
- We investigate the X-ray and mass structures in the merging galaxy cluster 1E0657-56.
- We first reproduce a clear off-set of an X-ray peak to a mass peak in N-body + hydrodynamical simulations.
- We discuss the ram pressure-stripping conditions in the mergers of two clusters with an NFW density profile using a simple analytic model.
 - ICM is more easily stripped from the smaller subclusters.
 - The ram pressure dominates the gravity of the substructure when the smaller cluster's mass is less than approximately one tenth of the larger cluster's mass.
- The characteristic X-ray and mass structures found in 1E0657-56 suggest that the mass ratio between the progenitors is close to the above-mentioned critical value.